



# Joint Relational Dependency Learning for Sequential Recommendation



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**Background**

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# WHAT IS RECOMMENDATION TASK?

**Input:** A user + her profile; An item + its Profile

**Output:** How likely she will adopt the target item? -> Relevance Score

Traditional Recommendation System:



## User Profile:

- User ID
- Rating history
- Age, Gender
- Clicks
- Income level

.....

## Item Profile:

- Item ID
- Description
- Image
- Category
- Price

.....

Long-term dependency  
Short-term dependency

Sequential recommendation

ignore to consider  
the **time information** of  
each interaction

# WHY SEQUENTIAL RECOMMENDATION?

Input: A user + her profile; An item + its Profile + Time information -> behavior sequence

Sequential Recommendation System:



# RELATED WORK

- BPR-MF[1]: long-term dependencies using matrix factorization method.
- GRU4Rec[2]: long-term dependencies using Gated Recurrent Units
- MARank[3]: models two types of short-term interactions with factorization model

## References:

[1] Rendle, S., Freudenthaler, C., Gantner, Z., Schmidt-Thieme, L.: BPR: Bayesian Personalized Ranking from Implicit Feedback (may 2012), <http://arxiv.org/abs/1205.2618>

[2]Hsu, K., Chou, S., Yang, Y., Chi, T.: Neural network based next-song recommendation. arXiv: Information Retrieval (2016)

[3]Yu, L., Zhang, C., Liang, S., Zhang, X.: Multi-Order Attentive Ranking Model for Sequential Recommendation. Proceedings of the AAAI Conference on Artificial Intelligence 33, 5709–5716 (2019). <https://doi.org/10.1609/aaai.v33i01.33015709>

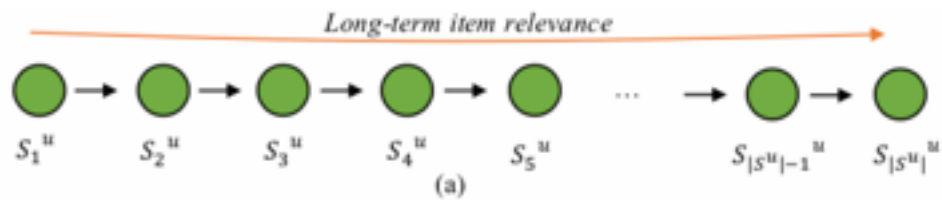
PART

**Driven idea**

TWO

# LEVEL OF DEPENDENCIES

long-term dependency:



capturing holistic dependencies of user-item sequence

→ **Collaborative Filtering (CF)** is the most well-known technique for recommendation.

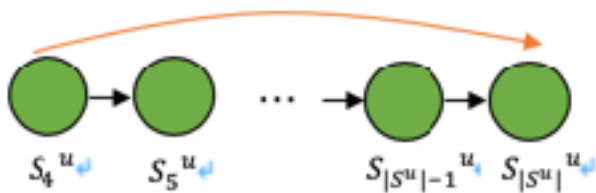
- Homophily assumption: a user preference can be predicted from his/her similar users.
- Pros: well-suited to train models that capture longer-term user preference profiles
- Cons:
  - 1) fail to exploit the rich information of transition dependencies of multiple items.
  - 2) enormous computing cost



# LEVEL OF DEPENDENCIES

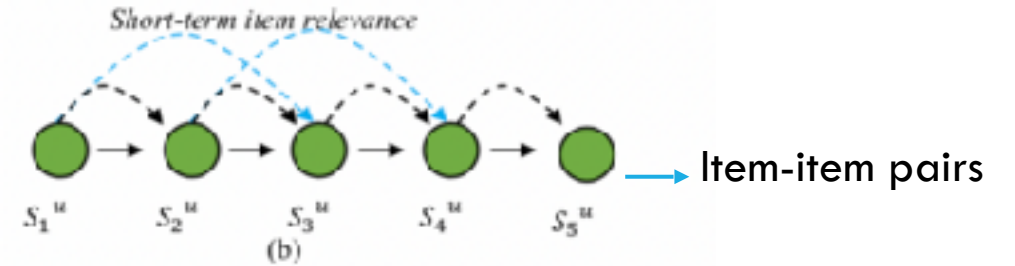
Individual-level dependencies:

Short-term dependency:

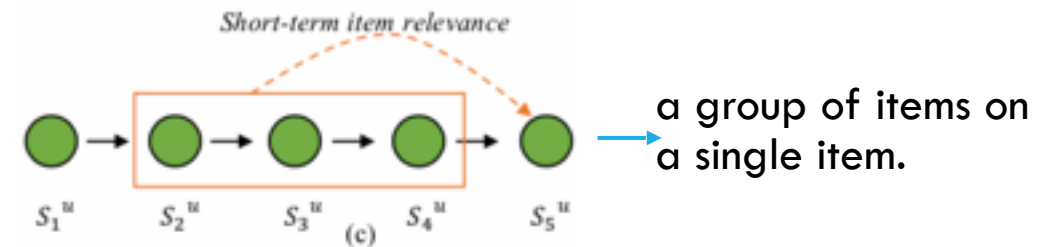
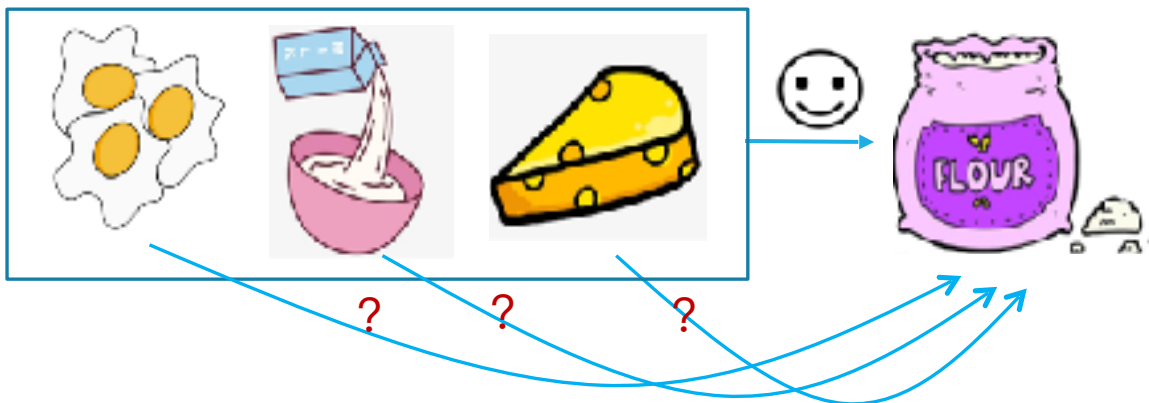


capturing partial dependencies within

A short time window.

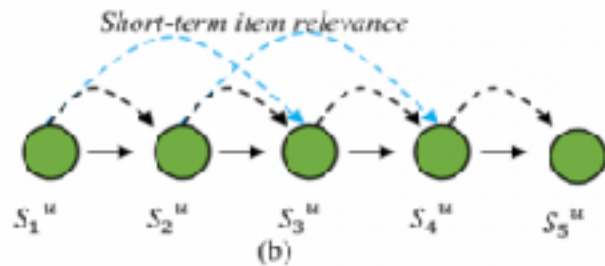


union-level dependencies



# LEVEL OF DEPENDENCIES

Individual-level dependencies:



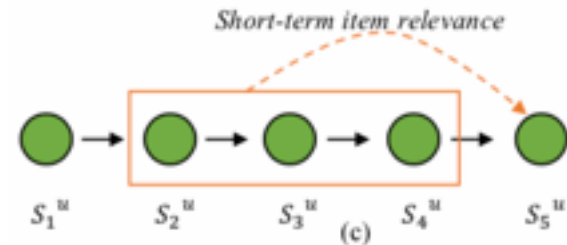
Pros:

- capture individual influence between a pair of single item
- rich in quantity

Cons:

- neglect the collective influence among three or more items

union-level dependencies



Pros:

- capture collective influence

Cons:

- sparsity problem

# WHAT WE DO?

## Problems:

- Modeling Long-term dependency only fails to exploit the information of transition dependencies of multiple items →
- enormous computing cost
- Individual-level dependency neglect the collective influence →
- sparsity problem of union-level dependency →

## Solutions:

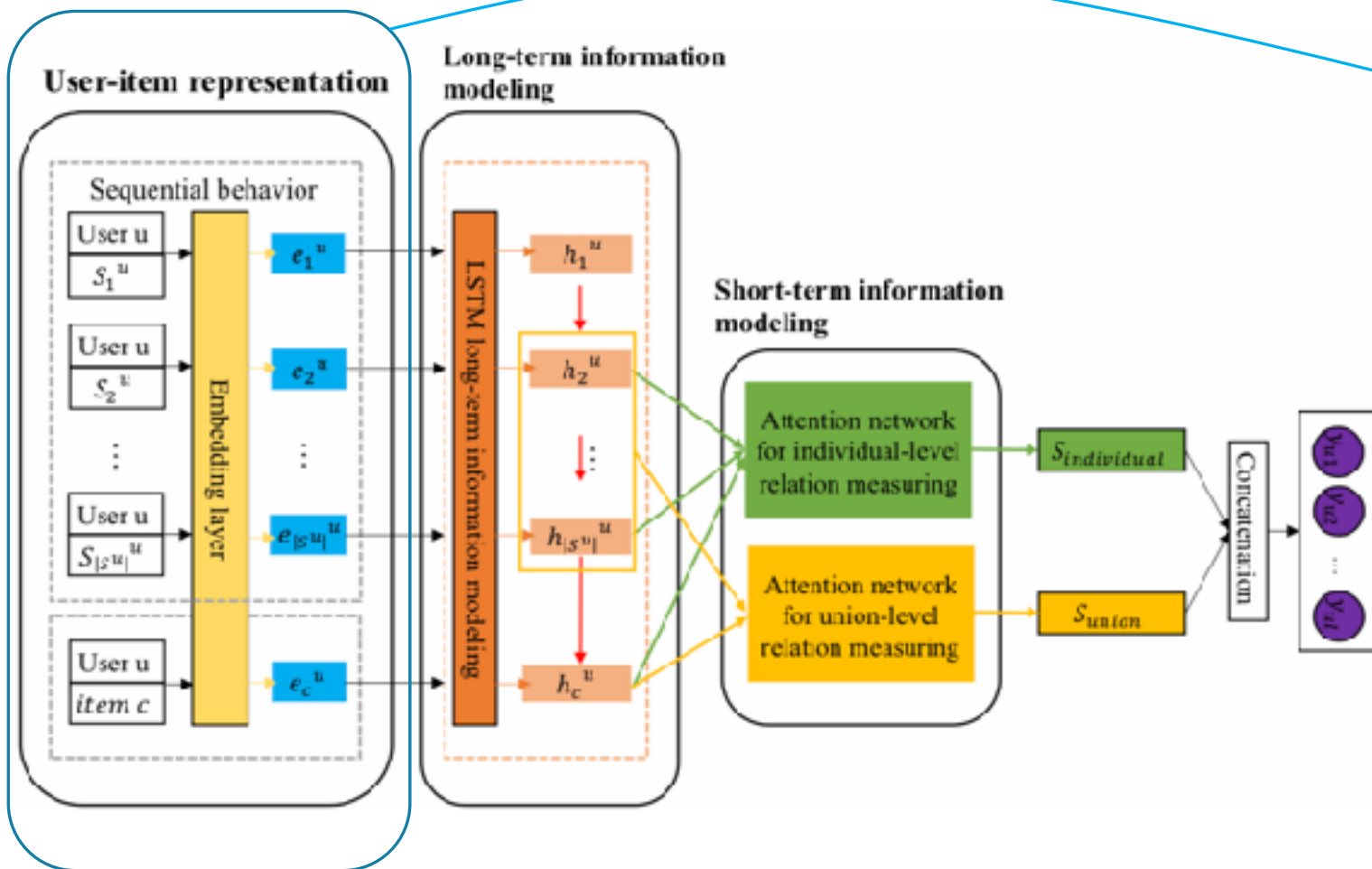
- Adding short-term dependencies
- Deep learning-based method
- Adding union-level dependencies
- Model individual-level relation and union-level relation together to address the sparsity

PART

**Methodology**

THREE

# UNIFIED FRAMEWORK:



## 1. User-item embedding

(Skip-gram Based Item Representation)

- apply skip-gram with negative sampling (SGNS) to generate **representation for each item** in user-item interaction sequence

### Input:

A sequence of interactions between U and I

$$\hat{S} = \{\hat{S}_j^{u_i} : u_i \in U\}, \hat{S}_j^{u_i} = (S_1^{u_i}, S_2^{u_i}, \dots, S_{|S_j^{u_i}|}^{u_i})$$

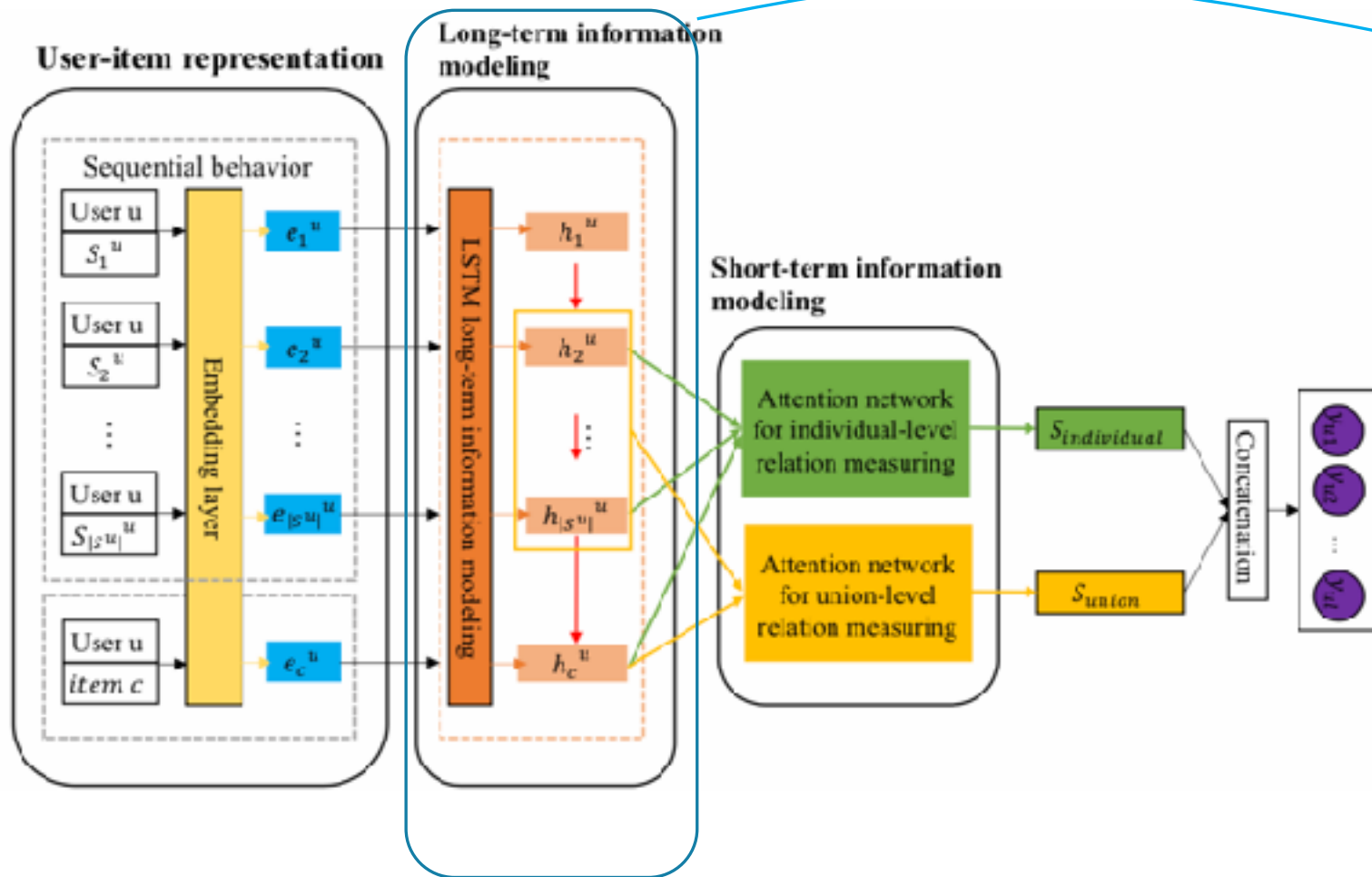
### Output:

$$L_c^{u_i}$$

$$P_u = e_1^{u_i}, e_2^{u_i}, \dots, e_{|S_j^{u_i}|}^{u_i}$$

$$e_c^{u_i}, e_{c_i}^{u_i} \in e_c^{u_i}$$

# UNIFIED FRAMEWORK:



## 2. Long-term Pattern modeling

- apply standard LSTM to model the dependency over the whole user-item interaction sequence

- Main equation:

$$h_i^u = g(e_i^u, h_{i-1}^u, W_{LSTM})$$

$e_1^{u_1}, e_2^{u_2}, \dots, e_{|S_j^{u_i}|}^{u_i}$   
 $h_1^{u_i}, h_2^{u_i}, \dots, h_{|S_j^{u_i}|}^{u_i}$

Each  $e_{c_i}^{u_i}$

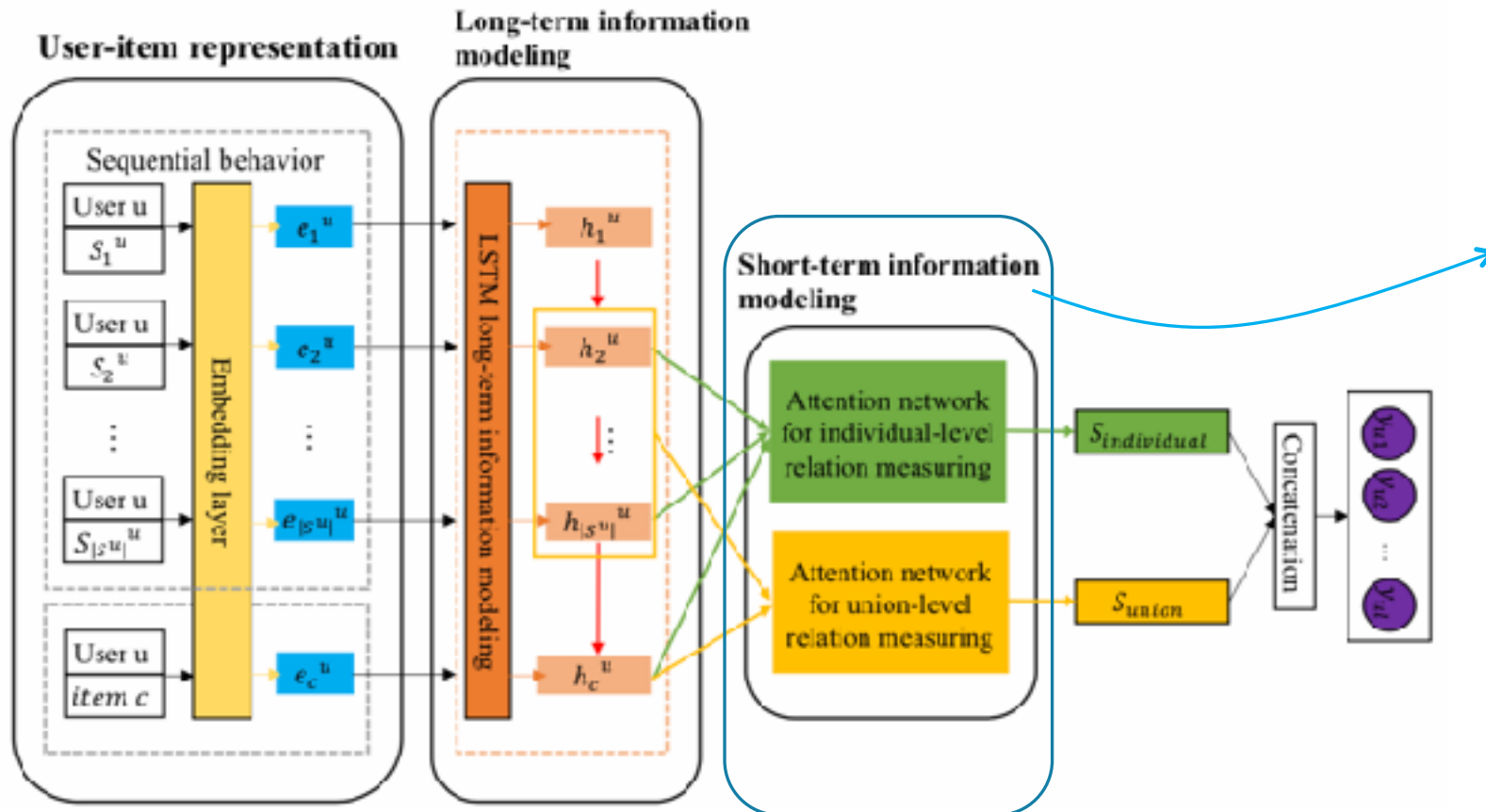
$$h_{c_i}^u = g(e_{c_i}^u, h_{|S^u|}^u, W_{LSTM})$$

$h_{c_i}^{u_i}$

- Output: long-term dependency - sensitive

$$h_1^{u_i}, h_2^{u_i}, \dots, h_{|S_j^{u_i}|}^{u_i} \quad h_{c_1}^{u_i}, h_{c_2}^{u_i}, \dots, h_{|c_i|}^{u_i}$$

# UNIFIED FRAMEWORK:



### 3. Multi-relational Dependency Modeling for Short-term Pattern

- Attention layer for individual-level relation measuring
- Attention layer for union-level relation measuring

$$h_1^{u_i}, h_2^{u_i}, \dots, h_{|S_j^{u_i}|}^{u_i}$$

$$h^{u_i}_{t-1}, h^{u_i}_{t-2}, \dots, h^{u_i}_{t-n} \quad (t - n < |S_j^{u_i}|)$$

Individual-level relation measuring:

- Input:

$$h^{(1)} = h^{u_i}_{t-1}, h^{u_i}_{t-2}, \dots, h^{u_i}_{t-n} \quad (t - n < |S_j^{u_i}|)$$

$$\bar{h}^{(2)} = (h_{c_1}^{u_i}, h_{c_2}^{u_i}, \dots, h_{|c_i|}^{u_i})$$

weights of the items in interaction sequence,

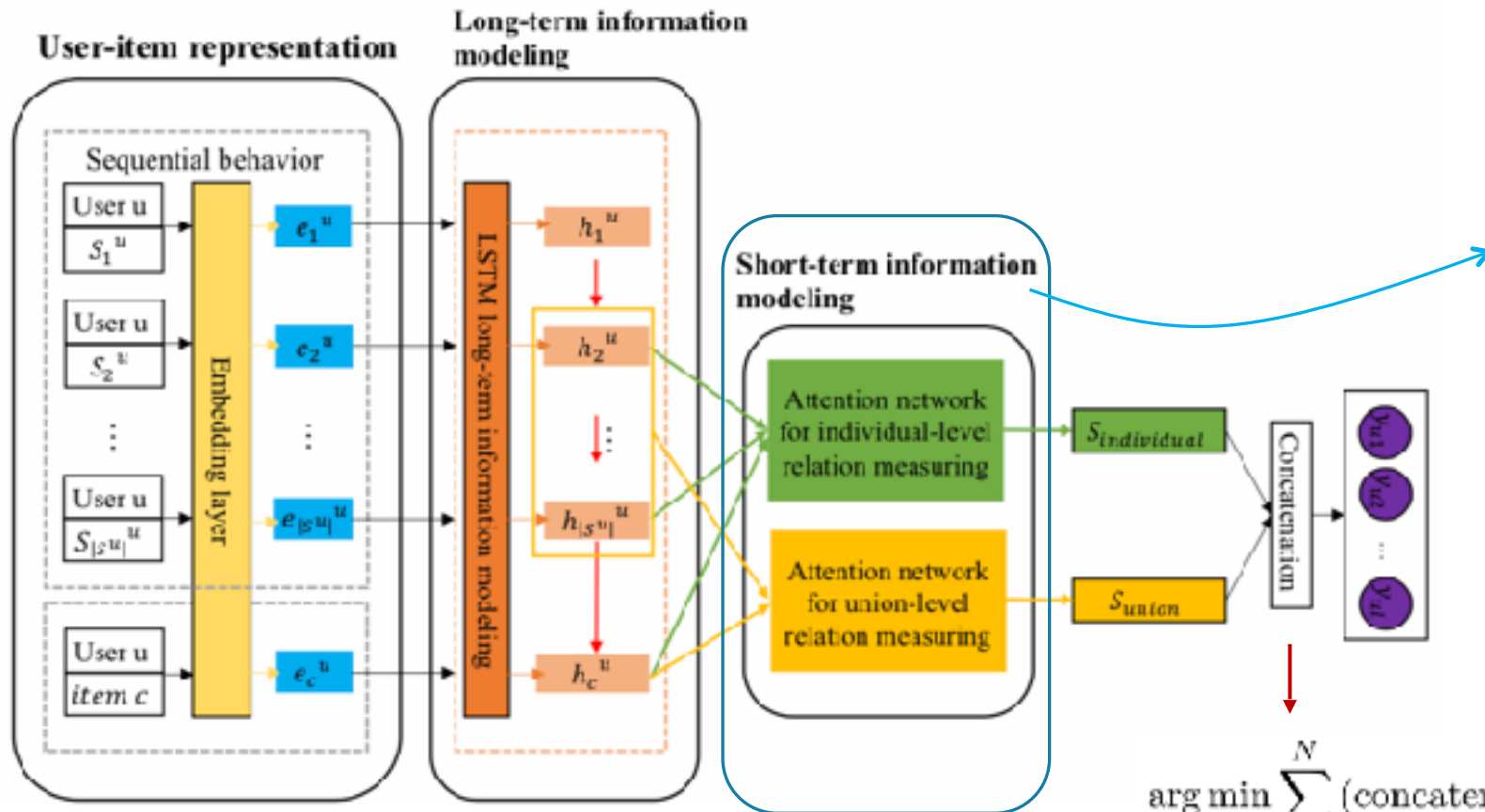
2. Calculate the likelihood of next items

$\alpha_i \in [0, 1]$  is the weight of  $h_{t-j}^{u_i}$  and  $h_{t-j}^{u_i} \in h^{(1)}$

$$s_k = \text{softmax}(\beta_1 h_{t-j}^{u_i} + \beta_2 h_{c_i}^{u_i} + b)$$

$$S_{\text{individual}} = \sum_{i=1}^{n-1} \alpha_i \cdot s_k$$

# UNIFIED FRAMEWORK:



Union-level relation measuring:

1. Learn the attention weights of the items in interaction sequence;
2. Calculate the likelihood of next items

$$s_m = \text{softmax}(\beta_3 W_i + \beta_4 h_{c_i}^u + b)$$

$$S_{union} = \sum_{i=1}^{n-1} \alpha_i \cdot s_m$$

$$\arg \min_{\Theta} \sum_{i=1}^N (\text{concatenate}(S_{individual}^{(i)}, S_{union}^{(i)}) - y_i)^2 + \frac{\lambda}{2} \|\Theta\|^2$$



PART

**Evaluation**

FOUR

# EXPERIMENT

## Movie&TV dataset :

Table 1. Statistical information of dataset.

Movies&TV	Users	Items	Interactions
before-processing	40929	51510	1163413
after-processing	35168	51227	1070645

## Results:

Methods	Movie&TV	
Measures@20	MRR	NDCG
BPR-MF	0.0089	0.0248
TranRec	0.0155	0.0392
GRU4Rec	0.0124	0.0344
FPMC	0.0162	0.0406
MARank	0.0170	0.0444
JDR-L	0.0179	0.0518
Improvement	5.2%	16.7%

## Baselines:

- BPR-MF: **matrix factorization** method for Sequential RS
- TranRec: typical **representation-based** Sequential RS
- GRU4Rec: **Gated Recurrent Unit** for sequential RS
- FPMC: Markov chain method modeling **individual item interaction**
- MARank: models **both individual-level and union-level interactions** with **factorization model**.

Methods	Movie&TV	
Measures@20	MRR	NDCG
LSTM-only	0.0154	0.0447
LSTM+ individual-level item interaction	0.0147	0.0442
LSTM+ union-level item interaction	0.0142	0.0423
JDR-L	0.0178	0.0518

PART

**Conclusion**

FIVE

# CONCLUSION

- We design a Joint Relational Dependency learning (JRD-L) for sequential recommendation.
- JDR-L model can unify both long-term dependencies and short-term dependencies from individual-level and union-level.
- Moreover, JDR-L can handle the sparsity problem when exploiting the individual-level relation information from the sequential behaviors.
- Extensive experiments on the benchmark dataset demonstrate the effectiveness of JRD-L.

**THANKS**